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Synthesis, crystal structures, substitutional and comparative structural analysis of copper diphosphates LiNaCuP₂O₇, LiKCuP₂O₇ and Rb_{0.5}Na_{1.5}CuP₂O₇

Ines Fitouri 🕩 and Habib Boughzala * 🕩

Laboratoire de Matériaux et Cristallochimie, Faculté des Sciences de Tunis, Université de Tunis El Manar, 2092 Manar II Tunis, Tunisia inesfitouri884@gmail.com (I.F.), habib.boughzala@ipein.rnu.tn (H.B.)

* Corresponding author at: Laboratoire de Matériaux et Cristallochimie, Faculté des Sciences de Tunis, Université de Tunis El Manar, 2092 Manar II Tunis, Tunisia. Tel: +216.98.595523 Fax: +216.72.220181 e-mail: habib.boughzala@ipein.rnu.tn (H. Boughzala).

RESEARCH ARTICLE



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ABSTRACT

The title compounds are members of the M₂O-CuO-P₂O₅ system (M = Li, Na, K and Rb), where the lithium, sodium, potassium, rubidium and cesium phases have already been structurally characterized. The studied diphosphates LiNaCuP₂O₇, LiKCuP₂O₇ and Rb_{0.5}Na_{1.5}CuP₂O₇ belong to a large family of materials of general formula, MM'CuP₂O₇ (M, M' = Monovalent cation) where the elements M and M' ionic radii are decisive in the structural type determination. They were synthesized by solid-state reactions. The X-ray structural analysis show that these compounds crystallize in the *P*2₁/*n* monoclinic lattice where the CuO₅ pyramidal square are linked to nearly eclipsed P₂O₇ groups by corner sharing to build up corrugated layers [CuP₂O₇]²⁻ extending perpendicularly to [O10]. The Li⁺, Na⁺, K⁺ and Rb⁺ cations reside in the interlayer space and in cavities delimited by the anionic network. In this study, the synthesis, the structure, the powder diffraction, the infrared spectroscopy, the thermal analysis (DTA/TGA) and a structural comparison are presented. The structural models were validated by Bond Valence-Sum (BVS) and charge distribution (CHARDI) analysis.

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1. Introduction

Many structures of copper diphosphates with general formula MM'CuP₂O₇ (M, M' = Monovalent cation), have been widely investigated in recent years because of their storage and energy conduction properties. Owing to the low density and the high reductive power of lithium metal, a great deal of interest has been focused on the development of lithium batteries as power source for portables devices or electric vehicles [1,2]. Indeed, in order to improve their ionic behavior, we attempted to partially replace the sodium and potassium cations in α -Na₂CuP₂O₇ [3] and K₂CuP₂O₇ [4] by smaller lithium cations. This substitution can be of interest for ionic conduction properties such as in rechargeable alkali batteries [5]. Currently, the increasing cost and the high toxicity of heavy metal based batteries encourage the pursuit of the Liion alternative. Thanks to environmental friendliness and natural abundance of sodium resources [6], Na-ion batteries are actually under intensive investigation.

The Cu²⁺ ion coordination flexibility, moving between the square pyramidal and the trigonal bipyramid, is able to modulate the phosphate anionic framework and incite to use copper to synthesize new materials.

2. Experimental

2.1. Synthesis and crystallization

The synthesis of the studied compounds was carried out starting with the adequate reagent mixed accordingly to the indicated relative proportions in Table 1. The mixtures were finely ground and heated in a porcelain crucible up to 623 K for 12 h to eliminate volatile components. The temperature was then increased to 873 K for LiNaCuP2O7, LiKCuP2O7 and 823 K for Rb_{0.5}Na_{1.5}CuP₂O₇ reaching the respective melting points and held for 15 days. The samples were slowly cooled (5 K/day) to 500 K and finally allowed to cool radiatively to room temperature. The products were washed with water and rinsed with a 0.5 M aqueous solution of HCl. Only one type of regular light-blue prismatic crystals was observed for each compound. The obtained crystals were ground and checked by powder X-ray diffraction. Rietveld analysis with the program TOPAS 4.2 [7] revealed a single-phase product of LiNaCuP₂O₇, LiKCuP₂O₇ and Rb_{0.5}Na_{1.5}CuP₂O₇. During the synthesis, no solid solution is observed in spite of the several attempts using different initial proportions.

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Compounds	Reagents		Proportion
LiNaCuP2O7	LiH2PO4 / NaH2PO4 / CuO		1:1:2:2
LiKCuP ₂ O ₇	LiH ₂ PO ₄ / KH ₂ PO ₄ / CuO		1:1:2:2
Rb _{0.5} Na _{1.5} CuP ₂ O ₇	Rb ₂ CO ₃ / NaH ₂ PO ₄ /CuO		2:1:1:2
Table 2 Crustallographic data and rai	finement parameters for compounds LiNa	CuBaO- LikCuBaO- and PhasNas (CuBaO	-
Crystal data	internent parameters for compounds Lina	CuP2O7, LINCUP2O7 and KD0.5Na1.5CuP2O	7.
Formula	LiNaCuP ₂ O ₇	LiKCuP207	Rb0.5Na1.5CuP2O7
Crystal system	Monoclinic	Monoclinic	Monoclinic
Space group	$P2_1/n$	$P2_1/n$	$P2_1/n$
a (Å)	4.988(2)	5.066(1)	7.817(2)
	13.598(4)	14.180(2)	9.806(3)
b (Å)	8.294(2)	8.473(7)	8.644(3)
c (Å) β (°)	8.294(2) 97.17(4)	8.473(7) 90.189(1)	
Unit-cell volume (Å ³)			104.48(2)
Z	562.1(3) 4	608.7(5) 4	641.6(3) 4
-	-	-	=
Calculated density (g/cm ³)	3.160	3.094	3.820
Absorption coefficient (mm ⁻¹)	5.262	4.784	11.57
Crystal size (mm)	0.32×0.09×0.13	0.16×0.09×0.13	0.11×0.06×0.13
Data collection		200 W	000 W
Temperature	398 K	398 K	398 K
Radiation, wavelength (Å)	ΜοΚα, 0.71073		
F(000)	516	548	696
θ_{\max} (°)	27	27	27
h, k, l ranges	-6→5, -2→17, -10→10	-6→5, -1→18, -10→10	-9→3, -1→12, -11→11
Measured reflections	2715	2765	2199
Independent reflections	1230	1323	1393
Reflections with $I > 2\sigma(I)$	1156	1201	1181
Refinement			
Refinement method	Full-matrix least-squares on F ²	Full-matrix least-squares on F ²	Full-matrix least-squares on F ²
R1(F), wR2(F ²)	1.9%, 5.9%	1.9%, 5.3%	2.8%, 7.4%
No. of refined parameters	112	112	116
GooF	1.12	1.00	1.08
(Δ/σ) max	< 0.001	< 0.001	< 0.001
$\Delta q_{\min}, \Delta q_{\max} (e. Å^{-3})$	0.86, -1.29	0.44, -0.36	0.69, -1.08

Table 1. Reaction mixtures made for each compound.

2.2. X-ray structure determination

A light blue single crystal has been selected for X-ray diffraction analysis from each preparation. Data collection was performed on an Enraf-Nonius CAD-4 diffractometer, operating at 298 K with (MoK_{α} radiation, $\lambda = 0.71069$ Å). An empirical ψ -scan absorption correction was applied in all of the three cases. The structures have been solved by direct methods using SHELXS-2014 software [8] and refined by leastsquare full-matrix based on F² using SHELXL-2014 [9] and SHELXLe [10] software. A summary of the crystallographic data and structural determination for LiNaCuP2O7, LiKCuP2O7 and Rb_{0.5}Na_{1.5}CuP₂O₇ is provided in Table 2. The final reduced atomic coordinates, the equivalent thermal factors and the refined partial occupancies are listed in Table 3. The geometrical characteristics are detailed in Tables 4 and 5. The crystallographic data are deposit in the ICSD database [11] and can be retrieved using the respective Collection Code 433889 for LiKCuP₂O₇, 433890 for LiNaCuP₂O₇ and 434654 for Rb0.5Na1.5CuP2O7.

The free variable restraint (SUMP) was required to restrain the sum of the monovalent cations occupation factors accordingly to the electro neutrality of the cell content. It's worthy to note that for LiNaCuP₂O₇ and LiKCuP₂O₇ the same cationic site 1 is preferred by the lithium and the site 2 is fully occupied by the sodium and the potassium respectively as it can be seen in Table 3. After minor alignment of the atomic coordinates in NaKCuP₂O₇ [12] particularly for O6 an O7, selected valance angles are summarized in Table 5.

The structural models are validated by the two structural tools, Bond Valence Sum (BVS) [13,14] and Charge Distribution analysis (CD) [15,16]. Both BVS and CD show expected valences (V) and charges (Q) of all the cation sites. The structural model is thus validated, as shown by the dispersion factor measuring the computed charges (Q) deviation in respect to the formal oxidation numbers. The

Bond Valence computation and Charge Distribution analysis are summarized in Table 6.

2.3. Infrared spectroscopy

The infrared (IR) transmission spectra of the compounds LiNaCuP2O7 and LiKCuP2O7 were studied using the Perkin-Elmer spectrophotometer in the range of 1400-400 cm⁻¹ wavenumbers containing the most significant solid state absorption bands. The samples were ground with 98% weight KBr and pressed (10 bar) into 10 mm diameter discs. The IR spectra of these two compounds presented in Figure 1 exhibit high similarity. The typical frequency ranges corresponding to symmetric (v_s) and asymmetric (v_{as}) P-O-P vibrational modes of the P₂O₇ group are centered at 773/914 cm⁻¹ for the compound LiNaCuP₂O₇ and 775/908 cm⁻¹ for LiKCuP₂O₇. The O-P-O bending and P-O stretching vibrational frequencies associated with the PO4 are shown in multiple bands in the 408-604 and 978-1044 cm⁻¹ range, respectively as shown in Table 7. To draw a parallel between the observed spectra of the tow compounds, the noted frequency shift towards the low frequencies for the bands associated to the symmetric deformation mode δ (O-P-O) and the asymmetric elongation mode v_{as} (P-O-P) can be explained by the sodium substitution by a heavier cation, the potassium.

2.4. Powder diffraction

Using the structural data obtained by single-crystal diffraction, the calculated powder X-ray pattern can be obtained using the Diamond 3 [17] program. On the other hand, the observed X-ray patterns were registered on a Bruker D8 Advance diffractometer using the $K\alpha 1/\alpha 2$ Copper radiation. The superposition of the observed and calculated raw diffraction of every compound reveals few weak unindexed Bragg pics and confirms the purity of the three synthesized phases.

next parameters $(^{\lambda_2})$ of atoms in the gradul structure of LiNaCuPaO- LiKCuPaO- and Pha-Na--CuPaO-

-	Cool unlates and isot	ropic displacement paral	neters (A ²) of atoms in the	crystal structure of LiNaCuP2O7, LiKCuP2O7 a	
Atom	X	У	Z	$U_{eq} = (1/3)\Sigma_i\Sigma_jU_{ij}a_i^*a_j^*a_i.a_j$	Occupancy
LiNaCuF	P207				
Li1	0.2398(8)	0.3018(3)	0.1573(5)	0.0154(15)	1.02(2)
Na1	0.2398(8)	0.3018(3)	0.1573(5)	0.0154(15)	0.03(2)
Li2	0.7691(2)	0.38605(8)	0.37307(2)	0.0175(4)	0.02(5)
Na2	0.7691(2)	0.38605(8)	0.37307(2)	0.0175(4)	1.004(5)
Cu	0.76586(5)	0.65856(2)	0.25798(3)	0.01163(13)	
P1	0.27162(2)	0.53003(5)	0.25517(6)	0.00830(15)	
P2	0.26202(2)	0.68581(4)	0.03920(6)	0.00685(15)	
01	0.1804(4)	0.42598(2)	0.2511(2)	0.0153(4)	
02	0.5623(3)	0.54255(2)	0.3156(2)	0.0129(3)	
03	0.0897(3)	0.59955(2)	0.34668(2)	0.0115(3)	
04	0.2614(3)	0.56959(2)	0.06942(2)	0.0103(3)	
05	0.3691(3)	0.70280(2)	-0.12657(2)	0.0101(3)	
06	-0.0249(3)	0.72131(2)	0.05316(2)	0.0105(3)	
07	0.4493(3)	0.72874(2)	0.17198(2)	0.0091(3)	
LiKCuP ₂					
Li1	0.2548(8)	0.3064(3)	0.1519(4)	0.0159(14)	1.02(2)
K1	0.2548(8)	0.3064(3)	0.1519(4)	0.0159(14)	0.02(2)
Li2	0.75511(2)	0.39822(3)	0.38239(6)	0.01542(18)	0.03(3)
K2	0.75511(2)	0.39822(3)	0.38239(6)	0.01542(18)	0.997(3)
Cu	0.73335(5)	0.65988(2)	0.23902(3)	0.01005(11)	
P1	0.25017(2)	0.53470(4)	0.23364(6)	0.00910(14)	
P2	0.24636(2)	0.69267(4)	0.03911(6)	0.00723(14)	
01	0.2182(3)	0.43118(2)	0.2169(2)	0.0182(4)	
02	0.5034(3)	0.56170(2)	0.31934(2)	0.0144(3)	
03	0.0190(3)	0.58294(2)	0.31455(2)	0.0140(3)	
04	0.2704(3)	0.58030(2)	0.05834(2)	0.0106(3)	
05	0.3576(3)	0.71637(2)	-0.12047(2)	0.0114(3)	
06	-0.0455(3)	0.71758(2)	0.05421(2)	0.0101(3)	
07	0.4138(3)	0.73352(2)	0.17365(2)	0.0101(3)	
	1.5 CuP 2 O 7				
Na1	0.4547(5)	0.5125(4)	-0.0634(5)	0.0390(11)	0.500(1)
Na2	0.5178(2)	0.14408(2)	0.16791(2)	0.0202(4)	1.004(9)
Rb	0.5000	0.5000	0.5000	0.0683(4)	0.495(2)
Cu	0.26021(5)	0.19311(5)	0.42517(5)	0.01255(16)	
P1	-0.10218(2)	0.33386(2)	0.29638(2)	0.0120(2)	
P2	0.15248(1)	0.35656(2)	0.11215(2)	0.0097(2)	
01	-0.1758(4)	0.4330(3)	0.3923(4)	0.0348(8)	
02	-0.2346(4)	0.2795(4)	0.1503(3)	0.0289(8)	
03	0.0027(4)	0.2188(3)	0.3929(3)	0.0240(7)	
04	0.0412(3)	0.4211(3)	0.2294(3)	0.0125(5)	
05	0.2729(4)	0.4684(3)	0.0894(3)	0.0203(6)	
06	0.0189(3)	0.3112(3)	-0.0387(3)	0.0160(6)	
07	0.2505(3)	0.2344(3)	0.2014(3)	0.0177(6)	



Figure 1. IR spectra of LiNaCuP2O7 diphosphates (in red) and LiKCuP2O7 (in blue).

This preliminary step is necessary to control the purity of the product, but remains limited because it is based on visual analysis and do not take care of the relative intensities of the reflections. The use of a more reliable method is crucial in a second step. In this context, a Rietveld study was carried out to identify discrepancies between the results obtained by the two techniques (single crystal and powder) and to ensure the purity of the studied material. Both GSAS [18] and TOPAS 4.2 [7] programs have been used to refine some structural parameters obtained by the single crystal diffraction investigation. The best profile fitting of the raw diffraction are plotted in Figures 2-7, respectively for the powders of $LiNaCuP_2O_7$, $LiKCuP_2O_7$ and $Rb_{0.5}Na_{1.5}CuP_2O_7$. In order to avoid obtaining incoherent values of the occupancy rates of the cations, restrictions have been applied on their respective sites, as well as a constraint respecting the electrical neutrality of the material.

Table 2 Coordinator and isotronic displa

LiNaCuP ₂ O ₇		LiKCuP ₂ O ₇		Rb _{0.5} Na _{1.5} CuP ₂ O ₇	
Li-01	1.888(5)	Li-01	1.863(4)	Rb-O1 viii	2.984(3)
Li-05 viii	1.978(4)	Li-05 viii	2.008(4)	Rb-O1 ix	2.984(3)
Li-07 ix	1.996(4)	Li-07 ix	1.998(4)	Rb-O6 ⁱ	3.077(3)
Li-06 vii	2.038(4)	Li-06 vii	2.068(4)	Rb-06 iv	3.077(3)
<li-0></li-0>	1.975(4)	<li-0></li-0>	1.984(4)	Rb-07 ⁱ	3.232(3)
				Rb-07 iv	3.232(3)
Na-01 ⁱ	2.384(2)	K-02	2.698(2)	Rb-05	3.563(3)
Na-02	2.405(2)	K-01 ⁱ	2.776(2)	Rb-O5 ×	3.563(3)
Na-03 v	2.411(2)	K-05 vi	2.808(2)	<rb-0></rb-0>	3.214(3)
Na-05 ^{viii}	2.451(2)	K-O3 iv	2.820(3)		
Na-07 ×	2.593(2)	K-06 ix	2.825(2)	Na1-05 vii	2.205(4)
Na-06 ix	2.633(2)	K-O2 iv	2.906(3)	Na1-05	2.211(4)
<na-0></na-0>	2.479(2)	K-07 xi	2.915(2)	Na1-03 xi	2.345(5)
		K-03 i	2.997(2)	Na1-03 iv	2.476(5)
Cu-03 i	1.924(2)	K-01	3.091(2)	Na1-02 v	2.653(5)
Cu-02	1.945(2)	<k-0></k-0>	2.870(2)	<na1-0></na1-0>	2.378(5)
Cu-07	1.956(2)				
Cu-O5 ⁱⁱ	2.167(2)	Cu-O3 ⁱ	1.920(2)	Na2-07	2.353(3)
Cu-06 ⁱ	2.199(2)	Cu-O2	1.940(2)	Na2-02 ix	2.383(3)
<cu-0></cu-0>	2.038(2)	Cu-07	2.003(2)	Na2-04 ii	2.447(3)
	(_)	Cu-O6 ⁱ	2.094(2)	Na2-01 ⁱⁱ	2.530(4)
P1-01	1.486(2)	Cu-O5 ⁱⁱ	2.211(2)	Na2-06 i	2.571(3)
P1-02	1.525(2)	<cu-0></cu-0>	2.033(2)	Na2-01 xi	2.595(4)
P1-03	1.531(2)		2.000(2)	Na2-03 xi	2.708(4)
P1-04	1.630(2)	P1-01	1.483(2)	<na2-0></na2-0>	2.512(3)
<p1-0></p1-0>	1.543(2)	P1-02	1.521(2)		
	1.010(2)	P1-03	1.521(2)	Cu-02 ⁱ	1.955(3)
P2-04	1.600(2)	P1-04	1.623(2)	Cu-07	1.959(3)
P2-05	1.511(2)	<p1-0></p1-0>	1.537(2)	Cu-O6 ⁱ	1.968(3)
P2-06	1.518(2)		1.007(1)	Cu-03	1.978(3)
P2-07	1.532(2)	P2-04	1.606(2)	Cu-05 ⁱⁱ	2.218(3)
<p2-0></p2-0>	1.540(2)	P2-05	1.504(2)	<cu-0></cu-0>	2.015(3)
	1010(1)	P2-06	1.526(2)		-1010(0)
		P2-07	1.532(2)	P1-01	1.484(3)
		<p2-0></p2-0>	1.542(2)	P1-02	1.516(3)
			1.542(2)	P1-02 P1-03	1.517(3)
				P1-04	1.627(3)
				<p1-0></p1-0>	1.536(3)
				<p1-02< td=""><td>1.330(3)</td></p1-02<>	1.330(3)
				P2-05	1.490(3)
				P2-06	1.519(3)
				P2-07	1.523(3)
				P2-04	1.620(3)
				<p2-0></p2-0>	1.538(3)

Table 4. Selected bond lengths (Å) in the crystal structures of LiNaCuP₂O₇, LiKCuP₂O₇ and Rb_{0.5}Na_{1.5}CuP₂O₇.

Symmetry code: (i) x+1, y, z; (ii) x+1/2, -y+3/2, z+1/2; (iii) -x+3/2, y+1/2, -z+1/2; (iv) -x+1, -y+1, -z+1; (v) x-1, y, z; (vi) -x+1, -y+1, -z; (vii) -x+1/2, y+1/2, -z+1/2; (vii) -x+1/2, y+1/2, -z+1/2; (vii) -x+1/2, y-1/2, -z+1/2; (vii) -x+1/2, -z+1/2; (vii) -x+1/2; (vii) -x+1/2



Figure 2. GSAS refinement of the LiNaCuP2O7.

If the profile and the background parameters functions are refined, the atomic coordinates and the thermal displacement parameters (obtained by the single crystal study) are fixed. Using the Table 8, a comparison of the main refined crystallographic parameters obtained by single crystal and powder diffraction can be done. Both results are close within the standard errors. Thus the crystal is representative of the powder.

2.5. Thermal analysis (DTA/TGA)

To have more information about the thermal properties of the studied compounds and particularly searching any solid state phase transition, coupled Differential Thermal Analysis (DTA) and Thermo Gravimetric Analysis (TGA) was performed on a Perkin Elmer STA6000 thermal analysis system using the polycrystalline samples of LiKCuP₂O₇ and Rb_{0.5}Na_{1.5}CuP₂O₇ in the range of 30 to 400 °C.

Bond	LiNaCuP ₂ O ₇	LiKCuP ₂ O ₇	NaKCuP ₂ O ₇	Rb0.5Na1.5CuP2O7	
03 ⁱ —Cu—02	90.36(7)	85.88(7)	91.46 (8)	02 ⁱ —Cu—07	160.14(1)
03 ⁱ —Cu—07	175.44(7)	174.75(6)	160.62 (8)	02 ⁱ —Cu—O6 ⁱ	94.62(1)
02—Cu—07	93.65(7)	89.17(7)	90.77 (7)	07—Cu—O6 i	86.87(1)
03 ⁱ —Cu—05 ⁱⁱ	90.68(7)	93.35(7)	92.15 (8)	02 ⁱ —Cu—03	83.69(1)
02—Cu—05 ⁱⁱ	135.57(7)	123.43(7)	109.22 (7)	07—Cu—O3	92.72(1)
07—Cu—05 ⁱⁱ	84.94(7)	87.91(6)	89.93 (7)	06 ⁱ —Cu—O3	173.85(1)
03 ⁱ —Cu—O6 ⁱ	92.36(7)	93.83(7)	91.34 (7)	02 ⁱ —Cu—05 ⁱⁱ	99.56(1)
02—Cu—06 i	140.50(7)	149.97(7)	176.22 (8)	07—Cu—O5 ⁱⁱ	100.03(1)
07—Cu—06 i	85.93(7)	91.34(6)	87.43 (7)	06 ⁱ —Cu—05 ⁱⁱ	95.09(1)
05 ⁱⁱ —Cu—O6 ⁱ	83.81(6)	86.59(7)	84.52 (7)	03—Cu—O5 ⁱⁱ	91.03(1)
01—P1—02	113.58(1)	112.72(1)	112.67 (12)	01—P1—02	114.6(2)
01—P1—03	114.35(1)	113.83(1)	114.78 (12)	01—P1—03	114.35(2)
02—P1—03	109.99(1)	108.72(1)	108.17 (11)	02—P1—03	111.06(2)
01—P1—04	107.11(1)	108.30(9)	107.95 (11)	01—P1—04	104.62(2)
02—P1—04	105.60(1)	106.31(9)	107.13 (10)	02—P1—04	106.04(2)
03—P1—04	105.47(9)	106.51(9)	105.64 (10)	03—P1—04	105.12(2)
05—P2—06	112.78(1)	112.93(9)	113.20 (10)	05—P2—06	115.07(2)
05—P2—07	111.64(1)	112.08(1)	111.96 (10)	05—P2—07	113.02(2)
06—P2—07	112.01(1)	112.59(9)	111.49 (10)	06—P2—07	110.79(2)
05—P2—04	107.23(9)	106.51(9)	107.91 (10)	05—P2—04	104.53(2)
06—P2—04	107.13(1)	107.12(8)	105.10 (10)	06—P2—04	106.88(1)
07—P2—04	105.56(9)	104.94(9)	106.66 (10)	07—P2—04	105.71(1)

Table 5. Selected angles (°) in the crystal structures of LiNaCuP2O7, LiKCuP2O7 and Rb0.5Na1.5CuP2O7.

Symmetry code: (i) *x*+1, *y*, *z*; (ii) *x*+1/2, -*y*+3/2, *z*+1/2.

Table 6. CHARDI and BVS analysis of ions in LiNaCuP₂O₇, LiKCuP₂O₇ and Rb_{0.5}Na_{1.5}CuP₂O₇.

			D7, LiKCuP2O7 and Rb0.5N		50 M(D)		
Ion	q(i).sof(i)	Q(i)	V(i).sof(i)	CN(i)	ECoN(i)	d _{ar} (i)	d _{med} (i)
LiNaCuP ₂ O ₇							
Li	1.00	0.98	1.02	4	3.89	1.974	1.975
Na	1.00	0.98	1.08	6	5.80	2.479	2.479
Cu	2.00	1.95	1.98	5	4.42	2.038	2.038
P1	5.00	4.99	4.93	4	3.84	1.543	1.543
P2	5.00	5.10	4.96	4	3.93	1.540	1.540
01	-2.00	-2.07	-1.88	3	3.00	1.919	1.913
02	-2.00	-2.05	-1.95	3	3.00	1.959	1.958
03	-2.00	-2.04	-2.00	3	3.00	1.955	2.207
04	-2.00	-1.79	-2.15	2	2.99	2.316	1.339
05	-2.00	-2.05	-1.99	4	4.00	2.702	2.027
06	-2.00	-1.86	-1.91	3	4.00	2.097	2.097
07	-2.00	-2.14	-2.08	4	4.00	2.019	2.202
LiKCuP ₂ O ₇							
Li	1.00	0.99	0.97	4	3.79	1.984	1.984
К	1.00	0.98	1.17	9	8.52	2.547	2.870
Cu	2.00	1.95	1.97	5	4.54	2.205	2.033
P1	5.00	4.96	4.97	4	3.85	1.538	1.537
P2	5.00	5.12	4.93	4	3.92	1.542	1.542
01	-2.00	-2.01	-1.63	4	3.79	2.304	2.040
02	-2.00	-2.02	-2.02	4	3.93	2.315	2.053
03	-2.00	-2.02	-2.00	4	3.90	2.266	2.146
04	-2.00	-1.98	-2.12	2	3.00	2.326	2.081
05	-2.00	-1.98	-1.73	4	4.00	2.132	2.132
06	-2.00	-1.99	-1.75	4	4.00	2.128	2.128
07	-2.00	-1.99	-1.80	4	4.00	2.111	2.286
Rb0.5Na1.5CuP2	207						
Rb	0.50	0.47	0.48	8	8.89	3.212	3.214
Na1	0.50	0.48	0.49	5	4.17	2.377	2.378
Na2	1.00	0.92	1.08	7	6.46	2.512	2.512
Cu	2.00	1.78	2.04	5	4.63	2.015	2.015
P1	5.00	4.7	4.98	4	3.83	1.535	1.536
P2	5.00	4.46	5.01	4	3.86	1.538	1.538
01	-2.00	-2.39	-1.79	3	4.19	2.551	2.398
02	-2.00	-2.14	-2.02	4	4.79	2.443	2.126
03	-2.00	-2.03	-2.01	4	4.63	2.204	1.798
04	-2.00	-1.88	-2.27	3	4.00	2.383	1.898
05	-2.00	-2.14	-1.94	4	3.00	1.968	2.031
06	-2.00	-2.47	-1.96	3	4.00	2.284	2.284
07	-2.00	-2.46	-2.00	3	4.47	2.581	2.266

The obtained results represented in Figures 8 and 9, proof that the compounds are thermally stable and exhibit no phase transition in the explored range of temperature.

3. Results and discussion

other hand, the $Rb_{0.5}Na_{1.5}CuP_2O_7$ structure presents some differences that should be explained.

3.1. The structural unit

The compounds $LiKCuP_2O_7$ and $LiNaCuP_2O_7$ exhibit the same structural arrangement with minor differences. On the

The structural units of the studied compounds are plotted on Figures 10. The PO_4 tetrahedra are almost regular, as evidenced by the bonds length and the valence angles grouped in Tables 4 and 5, respectively.

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 Table 7. Observed vibration frequencies (cm⁻¹) in LiNaCuP₂O₇ and LiKCuP₂O₇ and proposed assignments.

Observed frequencies		Assignments	
LiNaCuP ₂ O ₇	LiKCuP ₂ O ₇		
773	775	vs (P-O-P)	
914	908	v _{as} (P-O-P)	
411-604	408-598	δ (Ο-Ρ-Ο)	
982-1028	978-1044	ν (P-O)	

Table 8. Cell parameters and partial cationic occupancy refinements using single crystal and powder X-ray diffraction (GSAS and TOPAS) for compounds LiNaCuP₂O₇, LiKCuP₂O₇, and Rb_{0.5}Na_{1.5}CuP₂O₇.

Compound	LiNa	CuP2O7			LiKCuP ₂ O ₇				Rb _{0.5} Na _{1.5} CuP ₂ O ₇			
Method	Singl	e crystal	TOPAS	GSAS	Sing	le crystal	TOPAS	GSAS	Singl	e crystal	TOPAS	GSAS
Crystal system	Mono	oclinic										
Space group	$P2_1/r$	1										
a (Å)	4.987	7(2)	4.992(1)	4.991(9)	5.06	5(1)	5.072(7)	5.070(6)	7.817	(2)	7.826(1)	7.821(3)
b (Å)	13.59	97(4)	13.608(3)	13.606(3)	14.18	30(2)	14.205(2)	14.199(2)	9.806	(3)	9.822(2)	9.816(3)
c (Å)	8.293	3(2)	8.301(2)	8.299(2)	8.473	3(7)	8.487(1)	8.483(1)	8.644	(3)	8.662(2)	8.651(3)
β (°)	92.17	7(4)	92.1664(2)	92.1664(2)	90.1	39(1)	90.1864(1)	90.189(1)	104.4	8(2)	104.59(2)	104.48(1)
V (Å ³)	562.0)6(6)	563.62(3)	563.28(2)	608.	7(5)	611.56(2)	610.811(1)	641.6	(3)	644.430(2)	643.144(4)
Cationic	Li1	1.02(2)	0.939(2)	0.921(2)	Li1	1.02(2)	0.994(4)	0.996(4)	Na1	0.500(1)	0.498(1)	0.508(3)
sites	Na1	0.03(2)	0.061(2)	0.078(2)	K1	0.02(2)	0.006(4)	0.004(4)	Na2	1.004(9)	0.950(2)	1.015(4)
occupancies	Li2	0.02(5)	0.012(2)	0.015(2)	Li2	0.03(3)	0.003(4)	0.003(4)	Rb	0.495(2)	0.495(2)	0.502(6)
	Na2	1.004(5)	0.988(2)	0.984(2)	K2	0.997(3)	0.997(4)	0.997(4)				
Refinement												
Rint/Rexp (%)	2.70		2.26	2.25	3.10		1.63	1.63	2.40		1.51	2.48
wR/Rwp (%)	5.90		6.90	8.20	5.30		3.60	4.79	7.50		7.34	7.36
R/Rp (%)	1.90		4.20	5.42	1.90		2.60	3.41	2.80		4.63	4.65
GOOF	1.12		3.06	3.64	1.00		2.20	2.94	1.08		2.96	8.79





Figure 4. GSAS refinement of the LiKCuP₂O₇.

The phosphate polyhedra are linked by corner sharing O4 to form diphosphate groups P_2O_7 assembled with the copper pyramidal square CuO_5 by tow vertices O3 and O7. The $(CuP_2O_7)^{2-}$ units are linked together by vertices forming a corrugated anionic network.

3.2. The diphosphate group

Adopting a nearly eclipsed conformation, the O2–P2–P1– O7 dihedral angle is increasing when the alkaline atomic size decreases at the opposite to the bridging angle P2-O4-P1 as listed in Table 9.



Table 9. Values of the geometry index of the four compared diphosphates



The highest value of 123.033(7)° observed for Rb_{0.5}Na_{1.5}Cu P₂O₇ is comparable to that for NaCsCuP₂O₇ [19] 122.5(1)° (the largest value is noted for β -Rb₂CuP₂O₇ [20] 130.3(2)°). Within the diphosphate groups the bonds P1-O4 and P2-O4 are the longest since O4 is the bridging oxygen.

Every diphosphate group is linked to three copper polyhedra leaving only one free oxygen (01) pointing towards the empty space where the alkaline cations are lodged. The oxygen 01 charge (V(01).sof(01)) of -1.88, -1.63 and -1.79 in the three structures visible on Table 6 means that this oxygen is not involved in the anionic linkage and it's the first contributor in the cationic environment presenting the shortest distance Li-O, Na-O, K-O and Rb-O (see Table 4). One of the crucial differences between LiNaCuP2O7 (or LiKCuP2O7) and Rb_{0.5}Na_{1.5}CuP₂O₇ structures is that in the first one, this

corner O1 is located in direction of the base of the CuO_5 polyhedron (Figure 10a) and in the second one it is located in the apex side (Figure 10b.).

3.3. The copper polyhedron

The crystal structures of the title compounds contain one symmetrically independent copper site surrounded by five oxygens describing a distorted square pyramidal coordination. The four oxygens of the base of the pyramid are shared with two diphosphate groups and its apex is linked to a third P2O7 group. Two CuO₅ polyhedra are pointing their pyramidal apex in the same direction as shown in Figure 10a. On the other hand, in Rb0.5Na1.5CuP2O7 the same pair of connected copper polyhedra are pointing in opposite direction (Figure 10b).



Figure 8. Thermal analysis (DTA/TGA) of LiKCuP207.



Figure 9. Thermal analysis (DTA/TGA) of Rb_{0.5}Na_{1.5}CuP₂O₇.



Figure 10. Structural units in the crystal structures of LiNaCuP₂O₇ or LiKCuP₂O₇ (a) and Rb_{0.5}Na_{1.5}CuP₂O₇ (b). Symmetry code: (i): x-1, y, z; (ii): 0.5+x, 0.5-y, 0.5+z.

The described distorted pyramidal copper coordination is confirmed by the (4+1) bonds length and their angular values in Tables 4 and 5.

The τ parameter proposed by Addison [21] through the formula: $\tau = \frac{\beta - \alpha}{60} \approx -0.01667 \alpha + 0.01667 \beta$ was used to find

the appropriate polyhedral description of copper. β and α are the two greatest valence angles of the coordination center ($\beta > \alpha$) visible in Table 9. When τ is close to zero, the geometry is similar to square pyramidal and if τ is close to one the geometry is similar to trigonal bipyramidal. The computed values of τ parameter for the studied diphosphates and for

 $KNaCuP_2O_7$ [12] listed in Table 8, seem to be closely related to the monovalent cation size.

3.4. The structural packing

The 2-D structural arrangement of α -Na₂CuP₂O₇ is adopted by LiNaCuP₂O₇, LiKCuP₂O₇ and KNaCuP₂O₇. The crystal structure is build up by distorted CuO₅ square-pyramids linked to nearly eclipsed P₂O₇ groups by corners sharing leading to infinite chains running along (100) (Figure 11a). These ribbons are connected by the CuO₅ square-pyramids apex forming corrugated layers perpendicular to (010) direction (Figure 12).



Figure 11. Different orientations of copper coordination polyhedra along the chains of the anionic network: (a) in $LiNaCuP_2O_7$ structure, (b) in $Rb_{0.5}Na_{1.5}CuP_2O_7$.



Figure 12. Projection of the LiNaCuP₂O₇ structural model along [100], showing the corrugated interlayer space and zoom on small (S) and large (L) cations anionic environment.

The 2-D anionic stacking leaves interlayer empty space where the largest cations (L) are lodged and ellipsoidal cavities delimited by the vertices of the P_2O_7 and CuO_5 polyhedra housing the smallest cations (S). Figure 12 represents the structure projection along (100) direction where the crystallographic sites L and S are shown.

The crystal structure of the $Rb_{0.5}Na_{1.5}CuP_2O_7$ is also build up by distorted CuO_5 square-pyramids linked to P_2O_7 groups by corners sharing leading to infinite chains running along (101) (Figure 11b). At the opposite of the LiNaCuP_2O_7, where the copper square pyramid polyhedra apex are oriented in a common sense in this structure they are pointing in opposite direction. Thus, larger spaces are created able to lodge the Rb⁺. This double orientation leads to building undulated 2-D anionic framework and leaves empty interlayer space where and Na⁺ are lodged. A structure projection is plotted on Figure 13.

3.5. The cationic sites occupancies

The main important result deduced from this study and that of $KNaCuP_2O_7$ is the identification of two kinds of cationic sites in the structure. The first, located in the interlayer space, is booked for large cations (L) and the second for smaller one (S), having an ellipsoidal shape and delimited by the anionic network. Similar results related to the compounds with

general formula $A_3^1 M_3^{III}(XO_4)_4$ (A^I = Alkali metal, M^{III} = Al, Cr, Fe, ... X = As, P) were published by our team [22]. Nevertheless, in the structure of Rb_{0.5}Na_{1.5}CuP₂O₇ the interlayer space is more regular, thus the large Rb⁺ cation is lodged on a special position in large intersecting channels of the anionic framework with 50% occupancy. As observed in the studied compounds, the partial cationic site occupancy is a promising structural property offering a large interlayer space where the cationic mobility is possible. Thus, they can be potential candidates for interesting energy storage and conduction behavior. The complex impedance measurements of these compounds are underwork.

3.6. The structural filiation

Based on the content of the Table 10, a comparative study can be done between the members of the alkaline copper diphosphate family. The structures of LiNaCuP₂O₇, LiKCuP₂O₇, KNaCuP₂O₇ [12] and Rb_{0.5}Na_{1.5}CuP₂O₇ are similar to that of α -Na₂CuP₂O₇ [3]. Nevertheless, increasing the alkali cation size seems to introduce further symmetry, indeed, the Rb⁺ cation adopts a special position in the structure of Rb_{0.5}Na_{1.5}CuP₂O₇.

Accordingly, to the anionic 2D network topology, built up by linked $(CuP_2O_7)^{2-}$ units, the three studied compounds can be classified into the same group of selected copper diphosphates.

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Compound	Space group	a (Å)	b (Å)	c (Å)	Cell	Topology of	References
			β (°)		Volume (Å ³)	the anionic network	
Band structures							
Li ₂ CuP ₂ O ₇	I2/a	14.068(2)	4.8600(8)	8.604(1)	581.07(8)	1D	[23]
			98.97(1)				
Li ₂ CuP ₂ O ₇	C2/c	15.336(1)	4.873(1)	8.626(2)	585.24(16)	1D	[24]
			114.80(1)				
β-Na2CuP2O7	C2/c	14.728(1)	5.698(2)	8.067(1)	612.88(2)	1D	[25]
			115.15(1)				
Na1.12Ag0.88CuP2O7	C2/c	15.088(2)	5.641(1)	8.171(1)	624.48(2)	1D	[<mark>26</mark>]
			116.11(1)				
Layered structure							
LiNaCuP2O7	P21/n	4.988(2)	13.598(4)	8.294(2)	562.1(3)	2D	This work
			92.17(4)				
α-Na ₂ CuP ₂ O ₇	$P2_1/n$	8.823(3)	13.494(3)	5.108(2)	607.44(3)	2D	[<mark>3</mark>]
			92.77(3)				
LiKCuP ₂ O ₇	$P2_1/n$	5.065(1)	14.180(2)	8.473(7)	608.7(5)	2D	This work
			90.19(1)				
KNaCuP ₂ O ₇	$P2_1/n$	5.176(3)	13.972(5)	9.067(3)	655.6 (5)	2D	[12]
	P.0. /	=	91.34(2)	0.404400			
Rb _{0.5} Na _{1.5} CuP ₂ O ₇	$P2_1/n$	7.811(2)	9.789(3)	8.636(3)	641.6(3)	2D	This work
	51	0 500(4)	104.60(2)	5.05((0))	500.0(())	25	F 43
K ₂ CuP ₂ O ₇	Pbnm	9.509(4)	14.389(6)	5.276(2)	722.0(6)	2D	[4]
K ₂ CuP ₂ O ₇	$P42_1m$	8.056(2)	-	5.460(11)	354.35 (11)	2D	[27]
NaCsCuP ₂ O ₇	Pmn2 ₁	5.147(2)	15.126(3)	9.717(5)	756.5(5)	2D	[19]
Framework struct		F 102(0)	10.00((1)	15 14((2))	702 5 (2)	20	[20]
α-Rb ₂ CuP ₂ O ₇	Pmcn	5.183(8)	10.096(1)	15.146(3)	792.5(2)	3D	[28]
β-Rb2CuP2O7	Cc	7.002(1)	12.751(3)	9.773(2)	815.0(3)	3D	[20]
C C D O	C	7 4 (0 (()	110.93(3)	0.000(0)	005 0(12)	20	[20]
Cs ₂ CuP ₂ O ₇	Cc	7.460(6)	12.973(1)	9.980(8)	895.8(12)	3D	[29]
			111.95(1)				



Figure 13. 2-D crystal structure of Rb_{0.5}Na_{1.5}CuP₂O₇ projected along [101] direction with details of Rb⁺ and Na⁺ cations environments.

The character of binding of these structural units depends on the alkali metal cation and leads to various structural patterns. The increasing of the cationic size seems opening the diphosphate bridging angle and its dihedral angle. It contributes to reduce the copper coordination polyhedron distortion leading to slightly regular tetragonal pyramid as confirmed by τ values visible in Table 10. These effects are visible in Figures 12 and 13. Indeed, an attenuation of the interlayer space and the anionic sheets corrugation is clearly observed.

4. Conclusion

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Pure phases of $LiNaCuP_2O_7$, $LiKCuP_2O_7$ and $Rb_{0.5}Na_{1.5}$ CuP_2O_7 were synthesized by solid state reactions. Single crystal X-ray diffraction investigations revealed that these compounds crystallize in the P_{21}/n monoclinic space group and containing nearly eclipsed $P_{2}O_{7}$ diphosphate groups sharing corners with distorted pyramidal square CuO₅ arranged in layered stacking based on two-dimensional anionic network. Small cations prefer crystallographic site located in the interlayer space. Large cations are located in open ellipsoidal cavities situated in the intersection of empty channel delimited by the anionic network. The increasing of the cationic size seems opening the diphosphate bridging angle and its dihedral angle, reducing the copper coordination polyhedron distortion and attenuating the interlayer space and the anionic sheets corrugation. DTA and TGA results revealed the high thermal stability and the absence of any solid state phase transition. The shift observed in the main infrared vibration frequencies of the studied compounds confirms the crystallographic study. Using the structural data of the three compounds, the cell parameters and the cationic sites occupancies refinement using the Rietveld analysis leads to the same results obtained by the single crystal diffraction study. The same study proofs the high purity of the synthesized samples.

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Supplementary data

Further details of the crystal structures investigation are available from the Fachinformationszentrum Karlsruhe, D-76344 Eggenstein-Leopoldshafen, Germany, on quoting the depository number CSD-433889 for the compound LiKCuP₂O₇, CSD-433890 for LiNaCuP₂O₇ and CSD-434654 for Rb_{0.5}Na_{1.5} CuP₂O₇ the names of the authors and the citation of the paper.

Disclosure statement 💿

Conflict of interests: The authors declare that they have no conflict of interest.

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ORCID 回

Ines Fitouri <u>http://orcid.org/0000-0001-6428-3909</u> Habib Boughzala <u>http://orcid.org/0000-0002-7177-9934</u>

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EXAMPLE 1 Solve the sequence of the scope of the scope